

Remember:  
The most famous equation in the world:

$$E = mc^2$$

Mass can be converted to energy, and vice versa.

**Other decay modes**

**Beta-minus decay**

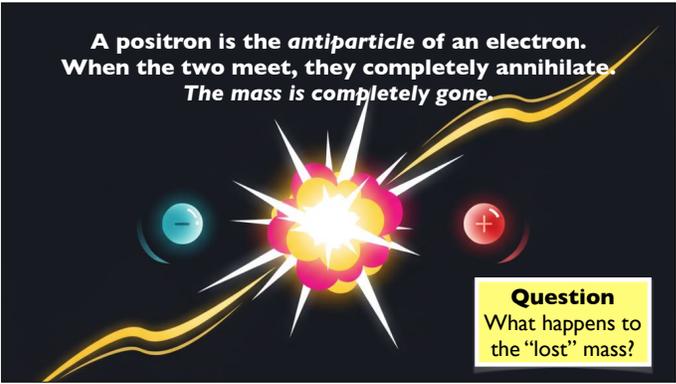
$${}^{14}_6\text{C} \Rightarrow {}^{14}_6\text{C} + e^-$$

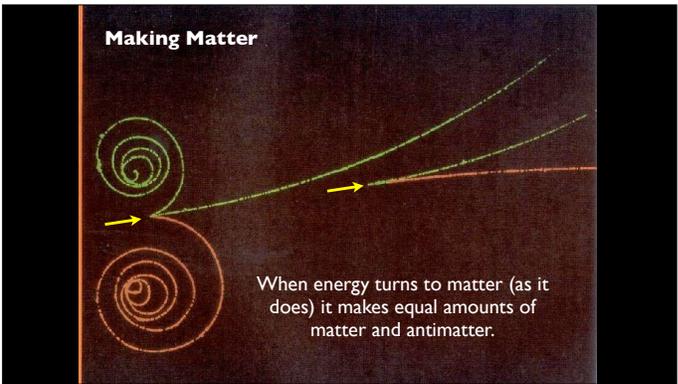
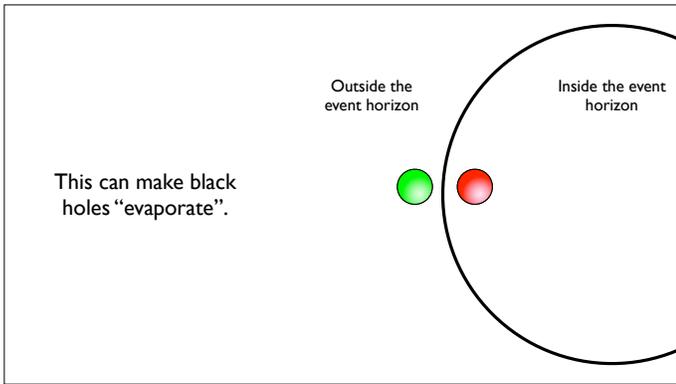
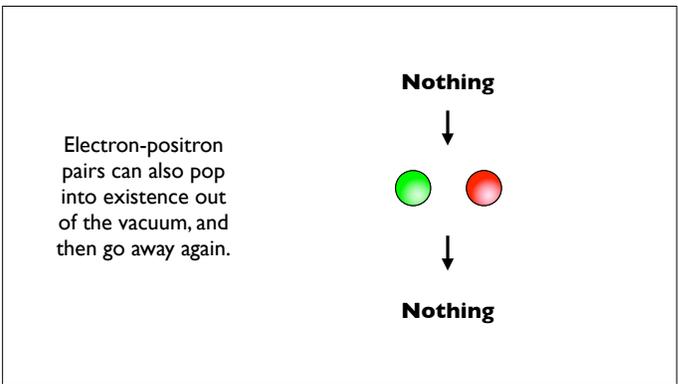
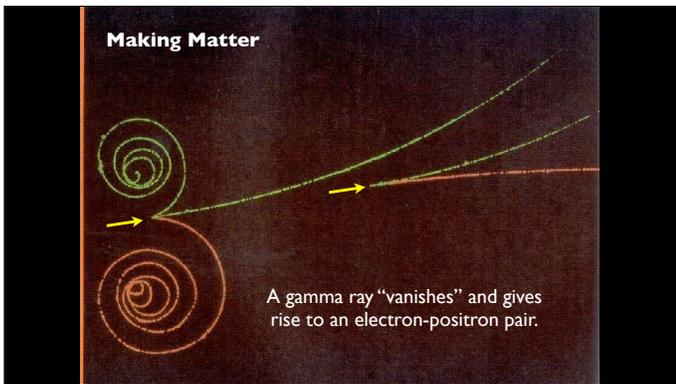
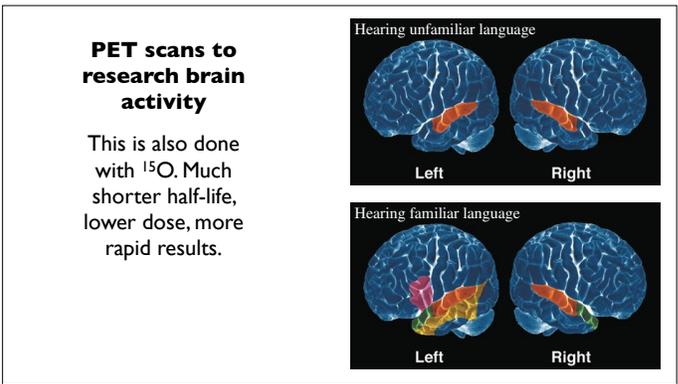
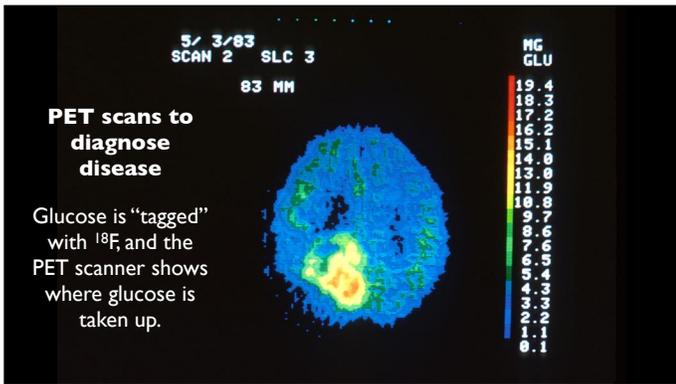
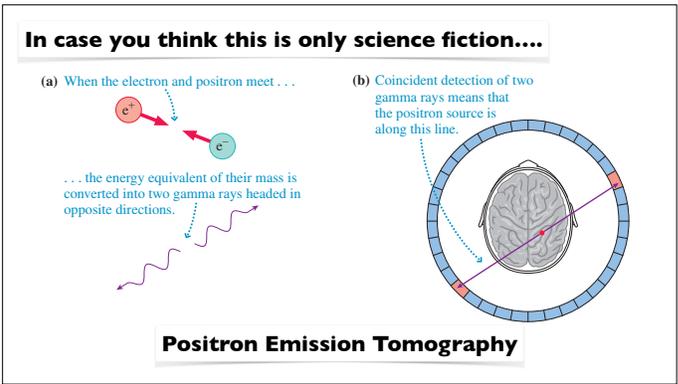
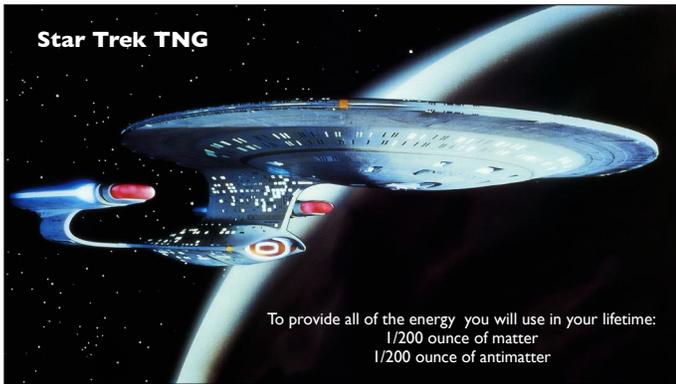
← **Electron**

**Beta-plus decay**

$${}^{18}_9\text{F} \Rightarrow {}^{18}_8\text{O} + e^+$$

← **Positron**





**Making Matter**

**Question**  
What problem does this raise?

So, the universe started out a ball of energy.  
And then some energy turned into matter and antimatter.  
But if you make matter and antimatter in equal amounts....

**Making Matter**

**A Puzzle**  
So why is there matter at all?  
Still working on that one....  
But there is evidence of an asymmetry.

**Making Matter**

**And....**  
Mostly, what was made was the lightest stuff. Electrons. Protons.  
**Hydrogen.**

**The Sun doesn't have a hard edge.**

Mercury

**As the universe expanded, density and temperature decreased.  
At some point, the matter became transparent.**

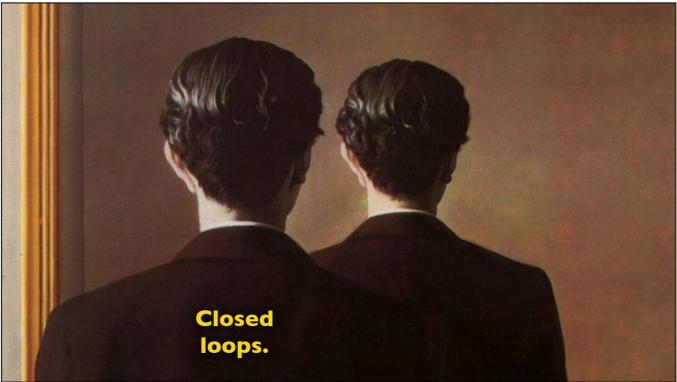
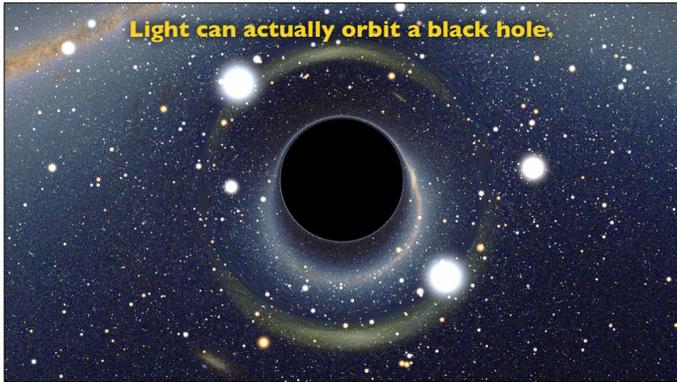
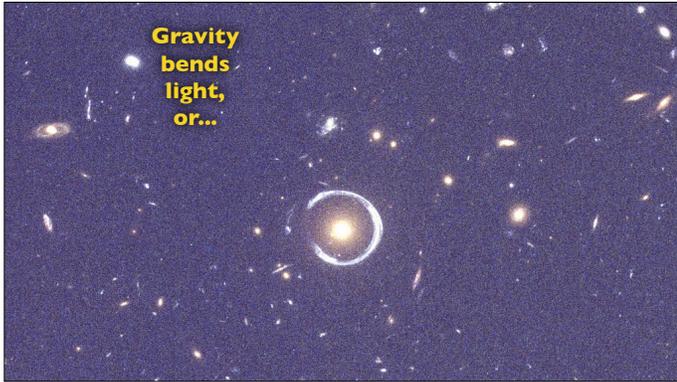
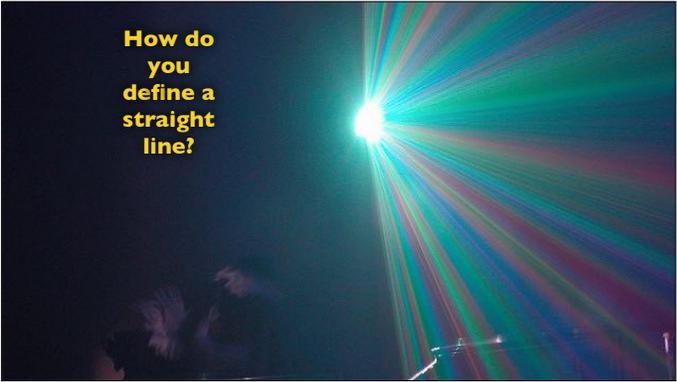
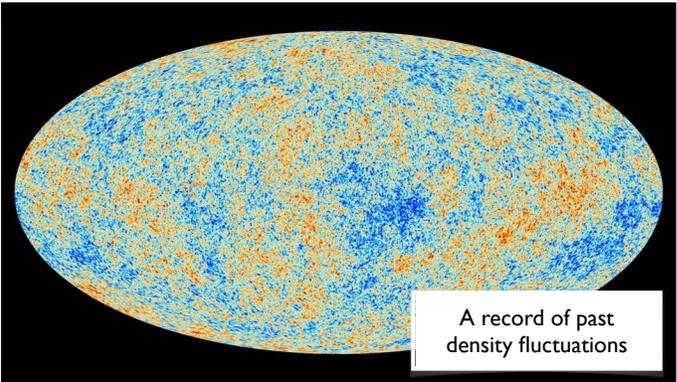
**At that time, the temperature of the universe was about the same as the temperature of the surface of the sun. So it was emitting visible light.**

**As time goes on, and the universe expands, the wavelength gets longer and longer.**

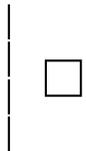
**Then: 500 nm**

**Now: 1,000,000 nm**

**You pick this up with radio telescopes.**

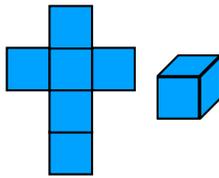


### A digression on topology.



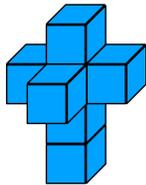
1 dimension  
4 lines

Fold to make a square  
Finite, no edge.



2 dimensions  
6 squares

Fold to make a cube  
Finite, no edge.



3 dimensions  
8 cubes

Fold to make a hypercube  
Finite, no edge.

**A universe that is finite, but with no edge.**



### Remembering High School Geometry

Perimeter / Area

**Question**  
What is the sum of the angles in a triangle?

### Remembering High School Geometry

Perimeter / Area

**Activity**  
On the balloon, can you make a triangle with 3 90° angles?

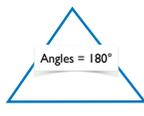
### Three Geometries, Three Destinies

**Spherical**



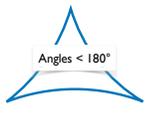
Angles > 180°

**Flat**



Angles = 180°

**Hyperbolic**



Angles < 180°

The curvature of space is determined by the amount of matter present. This determines the overall geometry of space too.

### Three Geometries, Three Destinies

**Spherical**



"Papa Bear" Universe:  
Too Much Mass

**Flat**



"Goldilocks" Universe:  
Just Right!

**Hyperbolic**



"Mama Bear" Universe:  
Too Little Mass

Gravity curves space. So the amount of gravity (and thus the amount of matter) determines the geometry. **And the destiny....**

### Three Geometries, Three Destinies

**Spherical**



The universe is finite, but there is no edge. It will expand for a while, then collapse.

**Flat**



The universe is infinite. It will expand forever.

**Hyperbolic**



The universe is infinite. It will expand forever.

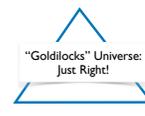
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This makes sense in terms of gravity, too. More means more gravity, which means more force opposing the expansion.

## Three Geometries, Three Destinies

**Spherical**



When the universe contracts, it will lead to a singularity—and perhaps another Big Bang?

**Flat**



Eventually, matter is so dispersed that stars and galaxies won't form. Things kinda fizzle.

**Hyperbolic**



Eventually, matter is so dispersed that stars and galaxies won't form. Things kinda fizzle.

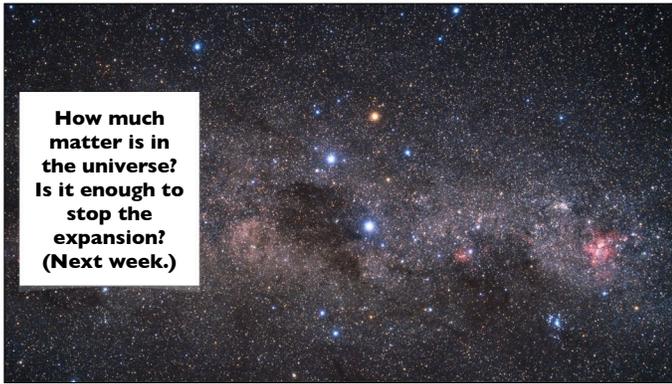
## The Big Crunch?

### Question

Clearly, we need a better name. What do you suggest?



**How much matter is in the universe? Is it enough to stop the expansion? (Next week.)**



**If the universe contracts, what happens to time? (You know, spacetime....) (Two weeks)**



**And all the other questions you might have. (Three weeks)**

